

1. D This is  $\frac{\frac{\sin x}{\cos x} + \frac{1}{\cos x}}{\frac{1}{\cos x}} = \sin x + 1$ .
2. B This represents the equations  $3a + 2b = 5$  and  $a + 4b = 6$ . The solution is  $a = 0.8$  and  $b = 1.3$ , so the sum is  $0.8 + 1.3 = 2.1$ .
3. C Because  $\alpha$  and  $\beta$  are in quadrants where the tangent function is negative, we may use right triangles to determine that  $\tan \alpha = -\frac{12}{5}$  and  $\tan \beta = -\frac{4}{3}$ . Using tangent addition formula, we have  $\tan(\alpha + \beta) = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta} = \frac{-56/15}{-11/5} = \frac{56}{33}$ .
4. B Let a point on this curve be  $(a, 2\sqrt{a})$ . Then, the distance to the point  $(6, 0)$  is  $\sqrt{(a-6)^2 + (2\sqrt{a}-0)^2} = \sqrt{a^2 - 8a + 36}$ . To minimize the distance, we need to minimize  $a^2 - 8a + 36$ , which occurs at the vertex where  $a = 4$ . The distance is then  $\sqrt{4^2 - 8 \cdot 4 + 36} = 2\sqrt{5}$ .
5. A As  $x \rightarrow \infty$ , the constants become negligible, so we have  $\sqrt{(x+1005)^2} - \sqrt{(x+5)^2} = (x+1005) - (x+5) = 1000$ .
6. C If  $x = 1$ , we have  $2t^2 + 8t + 9 = 1$ , so  $2(t+2)^2 = 0$  and  $t = -2$ . Thus,  $A$  is  $-2 + 3 = 1$ .
7. C Multiplying by 1 gives  $\frac{\sqrt{x+5}-3}{x-4} \cdot \frac{\sqrt{x+5}+3}{\sqrt{x+5}+3} = \frac{1}{\sqrt{x+5}+3} = \frac{1}{3+3} = \frac{1}{6}$ .
8. A After he picks three socks, if he does not have a pair, he has one of each color. Therefore, next sock must match one of the first three. He needs only to pull 4 from the drawer.
9. A All real numbers are also complex numbers (with an imaginary part of 0).
10. A  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ . Therefore, our probability is  $.25 + .5 - .75 = 0$ .
11. C This is a sphere with radius 3. A sphere has volume  $\frac{4\pi r^3}{3} = \frac{4\pi \cdot 27}{3} = 36\pi$ .
12. A Let  $x = 2^\omega$ . Then,  $x^2 - 3x + 2 = (x-1)(x-2) = 0$ . So,  $x = 1, 2$ . Considering the two cases:  $2^\omega = 1 \rightarrow \omega = 0$  and  $2^\omega = 2 \rightarrow \omega = 1$ . The sum is  $0 + 1 = 1$ .
13. D Expanding, we get  $(A)=(B)=(C)$ .  $\sin 2x \neq 1$ , so D isn't equal.
14. D The range of  $a^2$  is  $[0, \infty)$ , so this locus is a ray with initial point  $(2, 0)$ .
15. D Revenue = number of items sold  $\times$  price per item, so  $x(-.04x^2 + x + 1) = -.04x^3 + x^2 + x$ .
16. E This is an upwards opening parabola. As  $x \rightarrow \pm\infty$ ,  $f(x) \rightarrow \infty$ .
17. B  $\pi$  radians = 180 degrees. So,  $235^\circ \cdot \frac{\pi \text{ radians}}{180^\circ} = \frac{47\pi}{36}$ .
18. A Let the radius of  $A$  be  $a$  and the radius of  $B$  be  $b$ . Then,  $\frac{45}{360} \cdot 2\pi a = \frac{30}{360} \cdot 2\pi b$ , so  $3a = 2b$ , or  $a = \frac{2b}{3}$ . The ratio of the areas is  $\frac{\pi a^2}{\pi b^2} = \frac{a^2}{b^2} = \frac{4b^2}{9b^2} = \frac{4}{9}$ .
19. B  $121b = 1 + 2b + b^2 = (b+1)^2$ . So,  $(b+1)^2 = 144$ , so  $b+1 = 12$  and  $b = 11$ .
20. C At  $x = 1006$ ,  $-2x + 2010 < 0$ , so the graph is  $-(-2x + 2010) = 2x - 2010$ , which has slope 2.
21. C Let the length of the longer leg be  $x$ , and the shorter leg and hypotenuse be  $x-a$  and  $x+a$ , respectively. Then,  $2a = 2010$  and  $a = 1005$ . So,  $(x-a)^2 + x^2 = (x+a)^2$ , giving  $2x^2 - 2ax + a^2 = x^2 + 2ax + a^2$ , so  $x^2 = 4ax$ , and  $x = 4a = 4020$ . It is interesting to note that all triangles of the year must be 3-4-5 triangles; try proving this.

22. C From the Pythagorean Identities, we know that  $\sin^2 x + \cos^2 x = 1$ ,  $\sec^2 x - \tan^2 x = 1$ , and  $\cot^2 x - \csc^2 x = -1$ . The sum is then  $1 + 1 - 1 = 1$ .
23. B When  $x$  is in the domain of  $\ln x$  (as it is here),  $e^{\ln x} = x$ , so  $\frac{x}{x} = 1$ .
24. C Let the answer be  $k$ . Then,  $2x^2 = 7 + k$  and  $\frac{2}{x^2} = 7 - k$ . Hence  $\frac{2}{\frac{7+k}{2}} = 7 - k$ , so  $4 = 49 - k^2$ . Thus,  $k = \sqrt{45} = 3\sqrt{5}$ .
25. B By basic matrix operation definitions, we have that  $X = WZY^{-1}$ .
26. B There are no more in the 28000s, so we go to 29092. The sum of the digits is  $2+9+9+2=22$ .
27. C Converting to base 16,  $\log_{16}(a^2 + b^2) + \log_{16}(a^2 b^2) = \log_{16}(a^2 - 2ab + b^2) + \log_{16}(a^2 b^2)$ . Hence,  $a^2 + b^2 = a^2 - 2ab + b^2$ , so  $ab = 0$ . However, this is impossible for the domain  $a > 0, b > 0$ .
28. B Add them to get  $2f(a) = 10$ , so  $f(a) = 5$  and  $g(a) = 2$ . The product is 10.
29. B Plug in  $x = 0$  to get  $0 = a + b + c$ . Plug in  $x = -1$  to get  $-1 = d$ . The sum is  $-1$ .
30. A Cross-multiply to obtain the equation  $Ax + 2A + Bx + B = 12$ . So, since  $Ax + Bx = 0x$ ,  $A + B = 0$ . Substituting  $B = -A$ , we have  $2A - A = 12$ , so  $A = 12$ . Hence,  $AB = -12(12) = -144$ .